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## Discrete Mathematics Seminar

Time: Friday, 25 March 2016, 12:00 – 1:00 PM

Location: 237 Derrick Hall

Title: The Dehn–Sommerville Relations and the Catalan matroid

Speaker: Nicole Yamzon, PhD Student, San Francisco State University

### **Abstract:**

The  $f$ -vector of a  $d$ -dimensional polytope  $P$  stores the number of faces of each dimension. When  $P$  is simplicial the Dehn–Sommerville relations condense the  $f$ -vector into the  $g$ -vector, which has length  $\lceil \frac{d+1}{2} \rceil$ . Thus, to determine the  $f$ -vector of  $P$ , we only need to know approximately half of its entries. This raises the question: Which  $(\lceil \frac{d+1}{2} \rceil)$ -subsets of the  $f$ -vector of a general simplicial polytope are sufficient to determine the whole  $f$ -vector? We prove that the answer is given by the bases of the Catalan matroid.